

Exam 1 – Electrostatics

February 16, 2010

This is a closed book examination but during the exam you may refer to a 3"x5" note card with words of wisdom you have written on it. There is extra scratch paper available. Please explain your answers. Your explanation is worth 3/4 of the points on all questions.

A general reminder about problem solving:

<ul style="list-style-type: none"> • Focus <ul style="list-style-type: none"> ○ Draw a picture of the problem ○ What is the question? What do you want to know? ○ List known and unknown quantities ○ List assumptions • Physics <ul style="list-style-type: none"> ○ Determine approach – What physics principles will you use? ○ Pick a coordinate system ○ Simplify picture to a schematic (if needed) • Plan <ul style="list-style-type: none"> ○ Divide problem into sub-problems 	<ul style="list-style-type: none"> ○ Modify schematic and coordinate system (if needed) ○ Write general equations • Execute <ul style="list-style-type: none"> ○ Write equations with variables ○ Do you have sufficient equations to determine your unknowns? ○ Simplify and solve • Evaluate <ul style="list-style-type: none"> ○ Check units ○ Why is answer reasonable? ○ Check limiting cases! • Show All Your Work!
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The next two questions concern an electron (charge $-q_e$) and an alpha particle (charge $+2q_e$) that are separated by 16 nm in a region of space without any other charges.

1. [4 PTS] Compare the electrostatic force on the alpha particle, F_α , and the force on the electron, F_e .
- a) $4F_e = F_\alpha$
 - b) $2F_e = F_\alpha$
 - c) $F_e = 2F_\alpha$
 - d) $F_e = 4F_\alpha$
 - e) none of these

Explain:

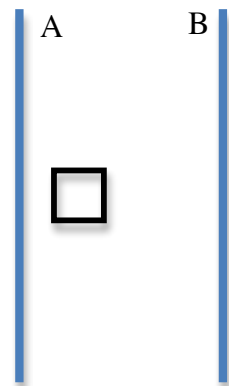
2. [4 PTS] The electron and alpha particle are moved apart so they are now separated by 33 nm.
- a) F_e increases and F_α decreases
 - b) F_e decreases and F_α increases
 - c) Both F_e and F_α decrease
 - d) Both F_e and F_α increase
 - e) none of these

Explain:

3. [4 PTS] A single point charge (Q) is located at the center of an imaginary sphere of radius 1 m and a much larger imaginary cylinder of diameter 2 m and side length 10 m. Compare the electric flux through each.
- The electric flux is zero through both the sphere and cylinder.
 - The magnitude of the electric flux is greater through the sphere.
 - The magnitude of the electric flux is greater through the cylinder.
 - There is the same positive electric flux through both the sphere and cylinder.
 - There is the same negative electric flux through both the sphere and cylinder.
 - None of these.

Explain:

The next two questions concern a hollow metal cube that is placed between two large charged plates. Both plate A and plate B are held at 90 volts. The plates are separated by 90 cm and the metal cube is placed 30 cm from plate A (so the cube is closer to plate A).



4. [4 PTS] The potential on the surface of the metal cube
- is 120 volts.
 - is 90 volts.
 - is 30 volts.
 - must be zero.
 - can not be determined. More information is needed.

Explain:

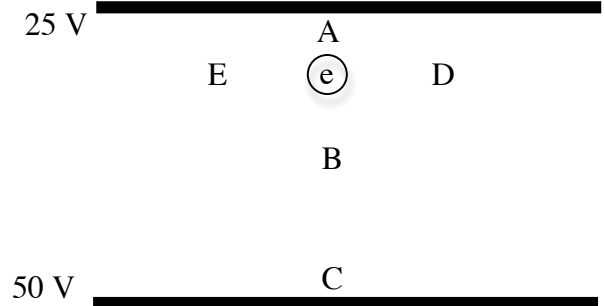
5. [4 PTS] The electric field inside the metal cube
- is proportional to $1/r^2$
 - is positive pointing towards plate A.
 - is zero.
 - is positive pointing towards plate B.
 - can not be determined without the size of the cube.

Explain:

6. [4 PTS] A large neutral metal disk is placed on an insulating post. A negatively charged balloon is brought near it - but does not touch it. The balloon is taken away. The disk is now
- charged but we cannot know its polarity.
 - neutral (has no net charge).
 - negatively charged.
 - positively charged.
 - none of these.

Explain:

7. [4 PTS] An electron is placed between two large plates held at different voltages. The electron is placed very close to the plate that is held at 25 volts.
- The electron moves towards A.
 - The electron moves to the middle (position B).
 - The electron moves toward C.
 - The electron oscillates between E and D.



Explain:

The next two problems can be done on the back of your exam or on additional paper.

8. [10 PTS] An electron that is initially at rest is placed between two parallel plates. At time $t = 0$ sec an electric field (0.5 kN/C) is turned on between the plates. Note: $q_e = -1.6 \times 10^{-19} \text{ C}$ and $m_e = 9.1 \times 10^{-31} \text{ kg}$.
- What is the velocity of the electron after it has traveled 30 cm ?
 - How long does it take to travel 30 cm ? NOTE: Think kinematics.
9. [10 PTS] A ball of negative charge has a constant charge density, $7.6 \times 10^{-3} \text{ C/m}^3$. The ball has a radius $R_B = 30 \text{ cm}$.
- Draw a graph of the electric field inside and outside the sphere?
 - What is the potential difference between $r_1 = 10 \text{ cm}$ and $r_2 = 20 \text{ cm}$?
 - What is the potential difference between $r_1 = 40 \text{ cm}$ and $r_2 = 60 \text{ cm}$?

Possibly useful mathematical relationships:

Law of Cosines $c^2 = a^2 + b^2 - 2ab \cos(\theta)$ which for $\theta = 90^\circ$ is the Pythagorean theorem $c^2 = a^2 + b^2$

Trigonometric identities:

$$\sin^2(\theta) + \cos^2(\theta) = 1$$

$$\sin(2\theta) = 2 \sin(\theta) \cos(\theta)$$

$$\cos(2\theta) = \cos^2(\theta) - \sin^2(\theta) = 2 \cos^2(\theta) - 1 = 1 - 2 \sin^2(\theta)$$

Derivative $\frac{d}{du} Cu^n = nCu^{n-1}$ and anti-derivative (integral) $\int Cu^n du = \frac{1}{n+1} Cu^{n+1} + \text{const.}$ of a polynomial

Derivative $\frac{d}{du} k \sin(au) = ka \cos(au)$ and integral $\int k \sin(au) du = -\frac{k}{a} \cos(au) + \text{const.}$ of the sine function

Derivative $\frac{d}{du} k \cos(au) = -ka \sin(au)$ and integral $\int k \cos(au) du = \frac{k}{a} \sin(au) + \text{const.}$ of the cosine function

The Chain Rule $\frac{d}{dz} f(u) = \frac{d}{dz} u \frac{d}{du} f(u)$